



# Business Calculus

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Alta Business Calculus was developed to meet the scope and sequence of a typical one semester Business Calculus course. To develop the course, Knewton used a variety of different source content, including OpenStax Calculus with added business applications, videos created by a Math Professor we have partnered with, and a team of Subject Matter Experts (SMEs). The SMEs come from diverse backgrounds and are all accomplished academics in the field of Mathematics.

Alta Business Calculus has two instructional sequences for every learning objective, giving students multiple opportunities to learn new concepts. Between our OpenStax with added business applications, video, and Knewton SMEs, we were able to solicit ideas from math instructors and students at all levels of higher education.

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## Business Calculus | Table of Contents

### Chapter 1: Linear Equations and Graphs

#### 1.1 Linear Equations and Inequalities

- Solve Linear Equations
  - Solve equations in one variable algebraically, variable just on one side
  - Solve equations in one variable algebraically, variable on both sides
- Interval Notation and Inequalities
  - Use interval notation
  - Use properties of inequalities
  - Solve simple inequalities in one variable algebraically
  - Solve compound inequalities in one variable algebraically

#### 1.2 Graphs and Lines

- Cartesian Coordinates
  - Plot ordered pairs in a Cartesian coordinate system
- Graphing Linear Equations
  - Graph equations by plotting points
  - Find x -intercepts and y -intercepts
  - Find the equation of vertical and horizontal lines
- Find and Understand Slope
  - Find the slope of a line given two points
  - Understand the relationship between the slope and y-intercept of a line and its equation
- Find Linear Equations
  - Find equation of a line, in slope-intercept form, given slope and one point
  - Find equation, in slope-intercept form, of a line passing through two given points
  - Given slope and intercept, find the equation of a line and write it in standard form
- Applications of Linear Equations
  - Set up a linear equation to solve a real-world application

#### 1.3 Linear Regressions

- Interpretations of Linear Functions
    - Interpret slope as a rate of change
  - Linear Regressions and Predictions
    - Find the linear regression equation given a list of data points
    - Make predictions using a line of best fit
-

## Chapter 2: Functions and Graphs

### 2.1 Functions

- Relations and Functions
  - Identify domain and range from a set of ordered pairs
  - Determine whether a relation represents a function
  - Use the vertical line test to identify functions
- Domain and Range
  - Find the domain of a function defined by an equation
  - Find the domain of a function defined by a graph
- Function Notation
  - Evaluate a function using function notation
  - Solve a function using function notation
  - Evaluate or solve a function from a table
  - Evaluate or solve a function from a graph
- Applications of Cost and Revenue Functions
  - Compute and relate profit, revenue, and cost functions

### 2.2 Elementary Functions and Graphs and Transformations

- Piecewise Functions and Graphs of Basic Functions
  - Define and graph six basic functions
  - Graph piecewise-defined functions
  - Evaluate piecewise-defined functions
- Transformations of Graphs
  - Graph functions using vertical and horizontal shifts
  - Graph functions using reflections about the x-axis and the y-axis
  - Graph functions using compressions and stretches

### 2.3 Quadratic Functions

- Quadratic Functions and the Parabola
    - Determine x- and y-intercepts of parabolas from a graph
    - Determine axis of symmetry and vertex of parabolas from a graph
    - Find the direction a parabola opens and its axis of symmetry and vertex from the general form of its equation
    - Find the domain and range of a quadratic function
  - Vertex Form of a Quadratic Function
    - Find the vertex and graph a parabola from a quadratic function given in vertex form
    - Write the equation of a quadratic function in standard form given the equation in general form
  - Quadratic Regression
    - Perform a quadratic regression with a calculator
    - Use the results of a quadratic regression to estimate values
-

- Applications of Quadratic Functions
  - Use quadratic functions in break-even and profit-loss analysis

## 2.4 Polynomials and Rational Functions

- End Behavior of Polynomial Functions
  - Identify power functions and polynomial functions
  - Identify if a graph is a polynomial function
  - Determine end behavior
- Local Behavior of Polynomial Functions
  - Identify intercepts of polynomial functions in factored form
  - Understand the relationship between degree, turning points, and x-intercepts
  - Understand the intermediate value theorem
  - Use factoring to find zeros of polynomial functions
  - Identify zeros and their multiplicities from an equation or a graph
- Graphs and Applications of Rational Functions
  - Solve applied problems involving rational functions
  - Find the intercepts of a rational function
  - Graph rational functions
  - Find the equation of a rational function from a graph
- Polynomial Regression
  - Perform a polynomial regression with a calculator
- Applications of Polynomial Functions
  - Solve real-world applications of polynomial equations

## 2.5 Exponential Functions

- Evaluate and Write Exponential Functions
    - Identify exponential functions
    - Evaluate exponential functions
    - Find the equation of an exponential function given the initial value and a point
    - Find the equation of an exponential function when the initial value is not known
  - Applications of Exponential Functions and Base  $e$ 
    - Find the equation of an exponential function in a word problem context
    - Calculate compound interest
    - Evaluate exponential functions with base  $e$
    - Calculate continuous growth and decay
  - Exponential Function Graphs
    - Graph exponential functions
    - Graph exponential functions using transformations
    - Find the equation of an exponential function given a graph
    - Write an exponential function from a description
  - Exponential Regression
    - Perform an exponential regression with a calculator
-

## 2.6 Logarithmic Functions

- Relate Logarithms and Exponents
  - Convert from logarithmic to exponential form
  - Convert from exponential to logarithmic form
- Evaluate Logarithmic Expressions
  - Evaluate logarithms with positive integer solutions
  - Evaluate logarithms with negative integer solutions
  - Use common logarithms
  - Use natural logarithms
- Logarithmic Function Graphs
  - Identify the domain of a logarithmic function
  - Graph logarithmic functions
  - Graph transformations of logarithmic functions
  - Write a logarithmic function from a description
- Basic Properties of Logarithms
  - Understand the basic properties of logarithms
  - Use the product rule for logarithms
  - Use the quotient rule for logarithms
  - Use the power rule for logarithms
- Rewrite Logarithmic Expressions Using Properties
  - Expand logarithmic expressions
  - Condense logarithmic expressions
  - Use the change-of-base formula for logarithms
- Solve Logarithmic Equations
  - Use the definition of a logarithm to solve logarithmic equations
  - Use logarithm properties and the definition of the logarithm to solve logarithmic equations
  - Use the one-to-one property of logarithms to solve logarithmic equations
- Logarithmic Regression
  - Perform a logarithmic regression with a calculator
- Applications of Logarithms
  - Applied logarithmic models

## Chapter 3: Limits and the Derivative

### 3.1 Introduction to Limits

- Limits From a Graph or Table
    - Understand the limit of a function and evaluate a limit from a table
    - Evaluate limits graphically
    - Understand the properties of limits
-

- Limits Analytically for Continuous and Piecewise Functions
  - Evaluate two-sided limits analytically for continuous functions
  - Evaluate limits analytically for piecewise functions
  - Evaluate limits analytically for absolute value functions
- Limits Analytically for Functions with Removable Discontinuities
  - Evaluate two-sided limits analytically for rational functions with removable discontinuities by factoring
  - Evaluate two-sided limits analytically for rational functions with removable discontinuities through expansion
  - Evaluate two-sided limits analytically for complex fractions with removable discontinuities
  - Evaluate two-sided limits analytically for rational functions that contain radicals with removable discontinuities

### 3.2 Infinite Limits and Limits at Infinity

- Infinite Limits
  - Evaluate limits analytically for functions with essential discontinuities
- Limits at Infinity
  - Evaluate limits of polynomial functions at infinity
  - Evaluate limits of rational functions at infinity
  - Evaluate limits of radical and exponential functions at infinity

### 3.3 Continuity

- Continuity and the Intermediate Value Theorem
  - Understand the definition of continuity
  - Distinguish between types of discontinuity
  - Understand and apply the intermediate value theorem
- Continuity of Piecewise Functions
  - Determine whether a piecewise function is continuous
  - Determine the value that makes a piecewise function continuous
- Rational and Quadratic Inequalities
  - Solve quadratic inequalities in one variable, graph the solution set, and express the solution set using interval notation
  - Solve inequalities that involve rational expressions, graph the solution sets, and express the solution set using interval notation

### 3.4 The Derivative

- Secant Lines and Average Rates of Change
    - Find the average rate of change given a function
    - Find the average rate of change given a table or graph
    - Find the average rate of change given a function and variable intervals
  - Tangent Lines and Instantaneous Velocities
    - Determine the sign of the slope of a line tangent to a function at a given point
    - Estimate the slope of the line tangent to a point on a curve
-

- Estimate the instantaneous rate of change of a function from successively closer approximations
- The Definition of the Derivative
  - Understand the limit definition of the derivative
  - Use the limit definition to find the derivative of a polynomial function
  - Use the limit definition to find the derivative of a rational function
  - Use the limit definition to find the derivative of a function with a radical

### 3.5 Basic Differentiation Properties

- The Power Rule and the Sum and Difference Rules
  - Use the constant, constant multiple, and power rule for monomials
  - Apply the sum and difference rules to combine derivatives
- Use the Power Rule to Explore Tangent Lines
  - Find the equation of the line tangent to a polynomial at a point
  - Determine where a function has a horizontal tangent
  - Determine the points on a function when tangent lines have a given slope

### 3.6 Differentials

- Differentials and Finding Error
  - Compute a differential
  - Estimate the amount of propagated and relative error using differentials

### 3.7 Marginal Analysis in Business and Economics

- Marginal Cost and Revenue
  - Compute and interpret marginal cost
  - Compute and interpret revenue and marginal revenue
- Marginal Average Cost and Revenue
  - Compute average cost and revenue
  - Compute and interpret marginal average cost

## Chapter 4: Additional Derivative Topics

### 4.1 Derivatives of Exponential and Logarithmic Functions

- Derivatives of Exponential Functions with Base  $e$ 
    - Find the derivative of an exponential function with base  $e$
    - Find the derivative of an exponential function with any base
  - Derivatives of Natural Log Functions
    - Find the derivative of a natural logarithmic function
    - Use properties of logarithms to find the derivative of a natural logarithmic function
  - Derivatives of Logarithmic Functions of Any Base
    - Find the derivative of a logarithmic function that is not base  $e$
    - Use properties of logarithms to find the derivative of a logarithmic function that is not base  $e$
-



- Logarithmic Differentiation
  - Use logarithmic differentiation
  - Use logarithmic differentiation with all properties of logarithms

#### 4.2 Derivatives of Products and Quotients

- The Product and Quotient Rules
  - Use the product rule to find the derivative of a function in the form  $f(x)g(x)$
  - Use the quotient rule to find the derivative of a function in the form  $f(x)/g(x)$
  - Use the product rule to find the derivative of a function in the form  $f(x)g(x)h(x)$
  - Combine the product and quotient rules with polynomials
- The Product and Quotient Rules with Exponential Functions
  - Use product and quotient rules to find the derivative of exponential functions with base  $e$
  - Use product and quotient rules to find the derivative of exponential functions with any base

#### 4.3 The Chain Rule

- Using the Chain Rule
  - Use the chain rule with the power rule
  - Use the chain rule with the product and quotient rules

#### 4.4 Implicit Differentiation

- Use Implicit Differentiation
  - Use implicit differentiation
  - Use implicit differentiation and the product rule
  - Use implicit differentiation to find the equation of a tangent line

#### 4.5 Related Rates

- Related Rates for Volume or Area Problems
  - Use related rates to solve problems involving volume
  - Use related rates to solve problems involving area
- Related Rates in Other Applications
  - Use related rates to solve problems involving distance
  - Use related rates to solve problems involving angles or shadows

#### 4.6 Elasticity of Demand

- Relative Rate of Change and Elasticity of Demand
    - Find the relative and percentage rate of change of a function
    - Compute elasticity of demand
    - Interpret elasticity of demand
-

## Chapter 5: Graphing and Optimization

### 5.1 First Derivative and Graphs

- First Derivative Test
  - Understand the relationship between the graph of a function and the sign of its derivative
  - Use the first derivative test to find local extrema from a graph
  - Use the first derivative test to find local extrema given a function
- The Graph of the Derivative Function
  - Estimate the value of a derivative at a point on a graph using a tangent line
  - Determine the open intervals where the first derivative is positive or negative from a graph
  - Determine the graph of the derivative function given the graph of a polynomial function

### 5.2 Second Derivative and Graphs

- Concavity and the Second Derivative Test
  - Determine concavity and find the inflection points from a graph of  $f(x)$
  - Determine concavity and find the inflection points given a function
  - Use the second derivative test to find local extrema given a function

### 5.3 L'Hospital's Rule

- Using L'Hospital's Rule
  - Apply L'Hospital's Rule in the  $0/0$  case
  - Apply L'Hospital's Rule in the (infinity/infinity) case
  - Determine when to apply L'Hospital's Rule

### 5.4 Curve Sketching Technique

- Sketch the Curve of a Function
  - Sketch the graph of a polynomial
  - Sketch the graph of a rational function
  - Sketch the graph of a function with a cusp

### 5.5 Absolute Maxima and Minima

- Extreme Value Theorem and Absolute Extrema
  - Understand the extreme value theorem
  - Locate local and absolute extrema from a graph
  - Locate critical points using derivatives
  - Locate absolute extrema

### 5.6 Optimization

- Applied Optimization Problems
    - Maximize or minimize area or volume
    - Minimize travel time
    - Maximize revenue
    - Minimize surface area
-

- Optimization Problems in the Abstract
  - Maximize the area of an inscribed rectangle
  - Maximize and minimize quantities given an expression with two variables
  - Minimize distance of a function to a point
- Optimization of Lot Size and Quantity
  - Find the economic lot or economic order quantity size which minimizes total cost

## Chapter 6: Integration

### 6.1 Antiderivatives and Indefinite Integrals

- Antiderivatives and the Integral
  - Find the antiderivative of a function
  - Understand integral notation and verify an indefinite integral
  - Understand the properties of indefinite integrals
  - Evaluate indefinite integrals involving constants or powers

### 6.2 Integration by Substitution

- Substitution and the Power Rule
  - Use substitution to find an indefinite integral with the power rule
  - Use substitution to evaluate a definite integral with the power rule

### 6.3 Differential Equations; Growth and Decay

- Basics of Differential Equations
  - Verify a solution of a differential equation
  - Identify the order of a differential equation
- Linear Differential Equations
  - Find a general solution to a linear differential equation
  - Find a particular solution to a linear differential equation
- Initial Value Problems
  - Verify a solution to a differential equation initial value problem
  - Solve a differential equation initial value problem
  - Solve applications of differential equation initial value problems
- Creating Direction Fields
  - Create a direction field for a first-order differential equation
  - Sketch a solution curve given a direction field
- Euler's Method
  - Use Euler's method to approximate the solution of a differential equation
- Differential Equations for Growth and Decay
  - Model and solve growth and decay applications with differential equations

### 6.4 The Definite Integral

- Left and Right Riemann Sums
    - Approximate the area under a curve using left-endpoint approximation
    - Approximate the area under a curve using right-endpoint approximation
-

- Midpoint and Trapezoid Rule
  - Approximate the area under a curve using midpoint approximation
  - Approximate the area under a curve using trapezoidal approximation
- Defining Definite Integrals
  - Explain the terms integrand, limits of integration, and variable of integration, and describe when a function is integrable
  - Evaluate an integral using the definition of the definite integral and left- or right-endpoint approximations
- Calculating Definite Integrals with a Geometric Approach
  - Use a geometric formula to calculate a definite integral
  - Calculate net signed areas under a line using formulas for area of a triangle
  - Calculate total area under a function using geometric formulas
- Properties of the Definite Integral
  - Use the properties of the definite integral

## 6.5 The Fundamental Theorem of Calculus

- Integrals and Derivatives with the Fundamental Theorem of Calculus
  - Use the Fundamental Theorem of Calculus to find the derivative of an integral function
  - Use the Fundamental Theorem of Calculus and the chain rule to find a derivative
  - Use the Fundamental Theorem of Calculus with two variable limits of integration
- Evaluating Definite Integrals with the Fundamental Theorem of Calculus
  - Evaluate definite integrals with the Fundamental Theorem of Calculus for functions with positive integer exponents
  - Evaluate definite integrals with the Fundamental Theorem of Calculus for functions with rational exponents
  - Evaluate definite integrals with the Fundamental Theorem of Calculus and the power rule by simplifying
- Average Value of a Function
  - Find the average value of a function over an interval

## Chapter 7: Additional Integration Topics

### 7.1 Area Between Curves

- Finding the Area of a Region Bounded by Two Curves
    - Find the area of a region between two linear functions
    - Find the area of a region bounded between a linear function and another function
    - Find the area of a region bounded between two curves
  - Finding the Area of Compound Regions
    - Find the area of a region bounded by two functions that cross
    - Find the area of a region bounded above by two different functions
  - Applications of Area Between Curves
    - Find and interpret the Gini index
-

## 7.2 Volume of Revolution

- Volume Using the Disk Method
  - Use the disk method to find the volume of a solid of revolution around the x-axis with polynomials or roots

## 7.3 Applications in Business and Economics

- Income Streams
  - Find the total income for a continuous stream
  - Find the present value of a continuous stream
  - Find the future value of a continuous stream
- Consumer and Producer Surplus
  - Find the consumers' surplus at a certain price level
  - Find the producers' surplus at a certain price level
  - Find the equilibrium price and the consumers' and producers' surplus at that price

## 7.4 Integration by Parts

- Basic Integration by Parts with Indefinite Integrals
  - Use integration by parts when  $u$  and  $v$  are given
  - Use integration by parts for indefinite integrals

## 7.5 Integration Using Tables

- Integration Tables
  - Use a formula from an integration table to evaluate an integral
- Integration with Computer Algebra Systems
  - Use a computer algebra system to evaluate an integral
- Reduction Formulas
  - Use a table with reduction formulas to evaluate an integral

## Chapter 8: Multivariable Calculus

### 8.1 Functions of Several Variables

- Introduction to Multivariable Functions
  - Evaluate a multivariable function
  - Sketch a point in three-dimensional space
  - Graph cross sections of a multivariable function

### 8.2 Partial Derivatives

- Partial Derivatives of a Function of Two Variables
    - Find the partial derivative of a function of two variables
    - Estimate the partial derivative of a function at a point from a graph or contour map
  - Total Differential
    - Use the differential to approximate the change in a function given the change in the inputs or to calculate maximum error
  - Partial Derivatives of a Function of Three or More Variables
    - Find the partial derivative of a function of three variables
-

- Higher Order Partial Derivatives
  - Find the higher order partial derivatives of a function of two variables
- The Chain Rule for Functions of Several Variables
  - Use the chain rule for one independent variable
  - Use the chain rule for two independent variables
  - Use the generalized chain rule

### 8.3 Maxima and Minima

- Critical Points and the Second Derivative Test for Functions of Two Variables
  - Find critical points of a function of two variables
  - Use the second derivative test to classify critical points of a function of two variables
- Absolute Extrema and Applications for Functions of Two Variables
  - Find the absolute extrema of a function of two variables on a closed region
  - Solve maximization and minimization word problems with multiple variables

### 8.4 Maxima and Minima Using Lagrange Multipliers

- Lagrange Multipliers with One Constraint
  - Use Lagrange multipliers to find maximum and minimum values of a function of two variables with a single constraint
  - Use Lagrange multipliers to find maximum and minimum values of a function of three variables with a single constraint
- Lagrange Multipliers with Two Constraints
  - Use Lagrange multipliers to find maximum and minimum values of a function with two constraints

### 8.5 Double Integrals over Rectangular Regions

- Iterated Integrals and Properties of Double Integrals
  - Recognize and use some of the properties of double integrals
  - Evaluate a double integral over a rectangular region by writing it as an iterated integral
  - Evaluate a double integral over a rectangular region by reversing the order of integration
- Applications of Double Integrals Over Rectangular Regions
  - Find the volume under a surface
  - Find the average value of a function over a rectangular region

### 8.6 Double Integrals over More General Regions

- Double Integrals Over Nonrectangular Regions
    - Recognize when a function of two variables is integrable over a general region
    - Evaluate a double integral by computing an iterated integral over a region bounded by two lines and two functions
  - Double Integrals by Decomposing Regions or Changing the Order of Integration
    - Evaluate a double integral over a more complex region by decomposing the region
    - Simplify the calculation of an iterated integral by changing the order of integration
-

- Applications of Double Integrals Over General Regions
  - Use double integrals to calculate the area of a general plane region
  - Use double integrals to calculate the volume of a region between two surfaces over a general plane region
  - Find the average value of a function over a general region

## Chapter 9: Trigonometric Functions

### 9.1 Trigonometric Functions Review

- Angles as Rotations and Radian Measures
    - Identify the measure of positive and negative angles in standard position and the quadrant of the terminal side
    - Convert between degree and radian measure of an angle
    - Understand when two angles are coterminal
  - The Six Trigonometric Ratios
    - Use right triangles to evaluate sin, cos, and tan functions
    - Evaluate reciprocal trig functions using right triangles or a sin, cos, or tan function
  - Sine and Cosine Values in the First Quadrant
    - Understand sin and cos values on the unit circle
    - Find exact sin and cos values for angles in the first quadrant of the unit circle
  - Sine and Cosine Values with Reference Angles and a Calculator
    - Find the reference angle for a given angle
    - Use reference angles to evaluate sin and cos functions
    - Use reference angles to find coordinates on the unit circle
    - Evaluate sin and cos functions with a calculator
  - The Other Trigonometric Ratios on the Unit Circle
    - Find the sec, csc, tan, and cot values for angles in the first quadrant of the unit circle
    - Use reference angles to evaluate sec, csc, tan, and cot functions
    - Evaluate trigonometric functions with a calculator
  - Use Given Trigonometric Ratios to Find Other Ratios
    - Understand the relationship between the quadrant in which an angle falls and the signs of the trig functions of that angle
    - Use the pythagorean identity
    - Find the values of all trigonometric functions given coordinates on a unit circle
    - Find the values of all trigonometric functions given the value of one trigonometric function
  - Characteristics of Sin and Cos Graphs
    - Graph the sin function and understand its properties
    - Graph the cos function and understand its properties
  - Applications of Trigonometric Functions
    - Use sinusoidal functions to solve real-world applications
-

## 9.2 Derivatives of Trigonometric Functions

- Derivatives with Trigonometric Functions
  - Find the derivative of a function with sine or cosine
  - Use the product or quotient rule to find a derivative with sine or cosine
  - Use the chain rule with trigonometric functions
- Applications of Trigonometric Derivatives
  - Compute derivatives of trigonometric functions in application problems

## 9.3 Integration of Trigonometric Functions

- Integration with Trigonometric Functions
  - Evaluate indefinite integrals involving trigonometric functions
  - Evaluate definite integrals involving trigonometric functions
  - Compute integrals of trigonometric functions in application problems

## Chapter 10: Differential Equations

### 10.1 Separation of Variables

- Finding Differential Equation Solutions using Separation of Variables
  - Find a general solution to a differential equation composed of two polynomials using separation of variables
  - Find a specific solution to a differential equation composed of two polynomials using separation of variables
- Application Problems using Separation of Variables
  - Solve solution concentration problems using separation of variables
  - Solve Newton's law of cooling problems using separation of variables

### 10.2 First-Order Linear Differential Equations

- Recognizing and Solving First-order Linear Differential Equations
  - Identify first-order linear differential equations
  - Write first-order linear differential equations in standard form
  - Solve a first-order linear differential equation using an integrating factor
- Applications of First-order Linear Differential Equations
  - Solve first-order differential equation problems about compound interest
  - Solve first-order differential equation problems involving equilibrium price

## Chapter 11: Taylor Polynomials and Sequences and Series

### 11.1 Taylor Polynomials

- Taylor and Maclaurin Polynomials
    - Recognize a Taylor series
    - Find the Taylor polynomials for a function at a value
-



## 11.2 Taylor Series

- Representing Functions with Taylor and Maclaurin Series
  - Represent a function at a value with a Taylor series and determine the interval of convergence
  - Find the Maclaurin series for a function and show that the series converges

## 11.3 Operations on Taylor Series

- Finding the Maclaurin Series that Represents a Function
  - Find the Maclaurin series for a trigonometric function
  - Find the Maclaurin series for a logarithmic or exponential function
  - Find a Maclaurin series by differentiating another series

## 11.4 Approximations Using Taylor Series

- Estimating Function Values with Taylor and Maclaurin Series
  - Find the Maclaurin polynomials for a function
  - Estimate a function value using Taylor polynomials
  - Determine the error of an estimated function value using Taylor's theorem
  - Estimate a trigonometric function value using Maclaurin polynomials
- Alternating Series and the Alternating Series Test
  - Determine if an alternating series converges or diverges using the alternating series test
  - Estimate the remainder of an alternating series
  - Determine whether a series converges absolutely or conditionally

## 11.5 Sequences and Series

- Geometric Sequences
    - Find the common ratio of a geometric sequence
    - Write terms of a geometric sequence
    - Write a recursive formula for a geometric sequence
    - Write an explicit formula for a geometric sequence
  - Applications of Series
    - Solve application problems with arithmetic series
    - Solve application problems with geometric series
    - Find the equivalent fraction for a repeating decimal
    - Solve an annuity problem
  - Finite and Infinite Geometric Series
    - Find the sum of a finite geometric series
    - Determine if the sum of an infinite series is defined
    - Find the sum of an infinite geometric series
  - Newton's Method
    - Use Newton's method to approximate the root of a polynomial
    - Use Newton's method to approximate a square root
    - Determine when Newton's method does not work
-

## Chapter 12: Probability and Calculus

### 12.1 Improper Integrals

- Improper Integrals over Infinite Intervals
  - Evaluate an improper integral over an infinite interval
  - Evaluate an improper integral from negative infinity to positive infinity

### 12.2 Continuous Random Variables

- Probability Density Functions
  - Understand the properties of probability density functions
  - Compute probability using a continuous probability density function
- Cumulative Distribution Functions
  - Understand the properties of a cumulative distribution function
  - Find the cumulative distribution function given a probability density function

### 12.3 Parameters of Continuous Random Variables

- Mean and Median of a Probability Density Function
  - Find the mean of a continuous probability density function
  - Find the median of a continuous probability density function
- Other Parameters of Probability Density Functions
  - Find the variance and standard deviation of a continuous probability density function

### 12.4 Special Probability Distributions

- Uniform Distribution
    - Compute probability using the uniform distribution
    - Compute the mean, median, and standard deviation of the uniform distribution
  - Exponential Distribution
    - Compute probability using the exponential distribution
    - Compute the mean, median, and standard deviation of the exponential distribution
  - Normal Distribution
    - Understand the notation and interpret the parameters of a normal distribution
    - Compute z-scores and use them to compare values from different data sets
    - Use a table to find probabilities in a normal distribution
-