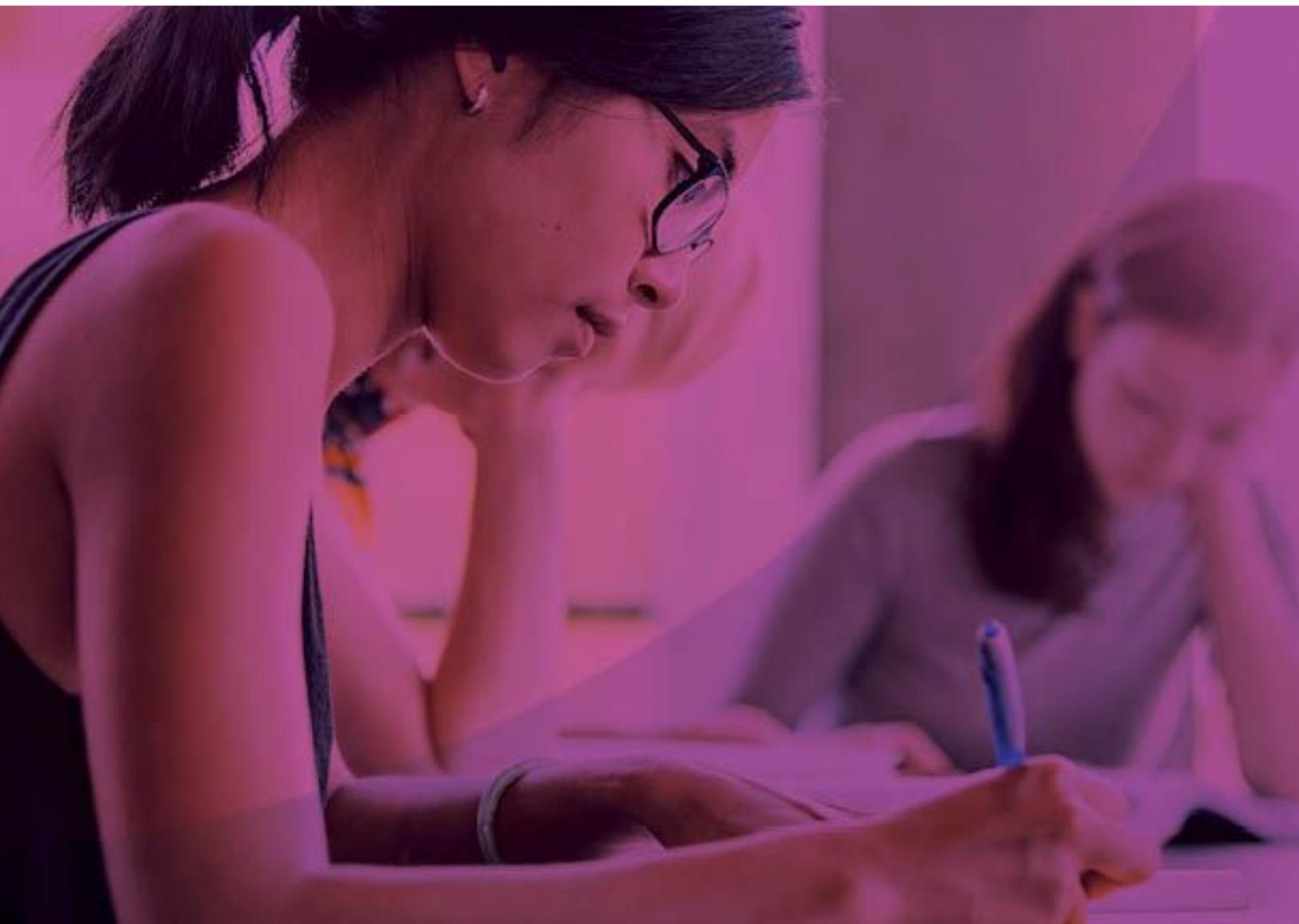




Finite Mathematics



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Source	Author(s) (Text or Video)	Title(s)	Link (where applicable)
OpenStax	Senior Contributing Authors: Gilbert Strang - Massachusetts Institute of Technology Edwin Herman - University of Wisconsin-Stevens Point	College Algebra and Statistics	OpenStax
Mathispower4u	James Sousa	MathIsPower4U	Mathispower4U Videos
Open Textbook Library		Math in Society	Math in Society

Alta Finite Mathematics was developed to meet the scope and sequence of a typical one-semester finite math course. To develop the course, Knewton used a variety of different source content, including OpenStax Calculus, a Math in Society textbook developed by a professor at Pierce College and the Open Course Library project, videos created by a Math Professor we have partnered with, and a team of Subject Matter Experts (SMEs). The SMEs come from diverse backgrounds and are all accomplished academics in the field of mathematics.

Alta Finite Mathematics has two instructional sequences for every learning objective, giving students multiple opportunities to learn new concepts. Between our text, video, and Knewton SMEs, we were able to solicit ideas from math instructors and students at all levels of higher education. Alta Finite Mathematics covers the typical breadth of topics, and also provides the necessary depth to ensure the course is manageable and engaging for instructors and students alike.

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Chapter 1: Algebra Reference

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