

# Finite Mathematics with Corequisite Support



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## Finite Mathematics with Corequisite Support | Table of Contents

### Chapter 1: Numbers and Operations

#### 1.1 Numbers and their Properties

- Ordering of Numbers
  - Order positive and negative numbers
  - Locate positive and negative numbers on the number line (\*15)
  - Find opposites
- Factors and Multiples
  - Identify multiples and apply divisibility tests
  - Find the prime factorization of a number
  - Find the least common multiple of two numbers
- Properties of Real Numbers
  - Understand the multiplication and division properties of zero
  - Identify additive and multiplicative inverses of a number
  - Use the commutative and associative properties
  - Identify rational numbers and irrational numbers
- Simplify Expressions Using Properties of Real Numbers
  - Simplify expressions by distributing a negative number
  - Simplify expressions using the distributive property
  - Simplify expressions using properties of identities, inverses, and zero

#### 1.2 Arithmetic Operations

- Addition and Subtraction of Integers
    - Subtract integers
    - Add integers
    - Add and subtract integers using order of operations
  - Division of Integers
    - Use division notation
    - Divide whole numbers using long division
    - Divide whole numbers using long division where there may be a remainder
    - Divide integers
  - Applications of Integer Multiplication and Division
    - Translate word phrases involving division to math notation
    - Multiply whole numbers in applications
    - Divide whole numbers in applications
  - Multiplication of Integers
    - Use multiplication notation
    - Multiply integers
    - Evaluate a whole number raised to a power and understand the terminology
-

- Multiplication
  - Translate word phrases involving multiplication to math notation

## Chapter 2: Fractions and Decimals

### 2.1 Introduction to Fractions

- Addition and Subtraction of Fractions
  - Add or subtract fractions with different denominators
  - Add or subtract fractions with a common denominator
- Mixed Numbers
  - Order fractions and mixed numbers
  - Model improper fractions and mixed numbers
  - Locate fractions and mixed numbers on the number line (\*37)
  - Convert between improper fractions and mixed numbers
- Equivalent Fractions
  - Simplify a fraction
  - Model equivalent fractions
  - Identify when fractions are equivalent
  - Find equivalent fractions
- Understanding Fractions
  - Understand the meaning of fractions
  - Locate fractions on a number line and write inequality statements involving fractions

### 2.2 Operations with Fractions

- Multiplication and Division of Fractions
  - Use the order of operations to simplify complex fractions and expressions with multiple operations
  - Translate an English phrase to an expression with fractions
  - Simplify expressions written with a fraction bar
  - Simplify complex fractions
  - Multiply fractions
  - Find reciprocals
  - Evaluate variable expressions with fractions
  - Divide two fractions
  - Divide fractions

### 2.3 Decimals

- Addition and Subtraction of Decimals
    - Perform operations with decimals
    - Locate decimals on a number line and write inequality statements involving decimals
    - Add and subtract decimals
-

- Decimals and Fractions
  - Simplify expressions with fractions and decimals
  - Convert between fractions and decimals
- Multiplication and Division of Decimals
  - Multiply decimals
  - Divide decimals

### **Chapter 3: Expressions and Equations**

#### 3.1 Building Expressions

- Introduction to Expressions
  - Identify expressions and equations
- Writing Expressions
  - Write word phrases from applications as algebraic expressions
  - Translate word phrases to expressions with integers
  - Translate word phrases to algebraic expressions

#### 3.2 Evaluating Expressions

- Evaluating Expressions with Numbers
  - Identify coefficients and identify and combine like terms
  - Evaluate an expression
  - Simplify an expression using order of operations
  - Simplify expressions with integers using order of operations
  - Evaluate a variable expression with integers
- Absolute Value
  - Simplify an expression involving absolute value using order of operations
  - Evaluate an absolute value expression

#### 3.3 Equations

- Solving Inequalities
    - Solve an inequality using the division and multiplication properties of inequality
    - Solve an inequality using the subtraction and addition properties of inequality
    - Solve one-step applications with linear inequalities
    - Solve a formula for a specific variable
  - Applications of Equations
    - Use the subtraction and addition properties of equality to solve application problems
    - Use the division and multiplication properties of equality to solve application problems
    - Use a problem-solving strategy for word problems
    - Solve a number problem
  - Solving Equations with Fractions and Decimals
    - Solve an equation involving fractions by eliminating the fractions and other steps
    - Solve an equation involving fractions by eliminating the fractions
-

- Solving Equations using Multiplication and Division
  - Translate an English sentence to an algebraic equation and solve using the division and multiplication properties of equality
  - Solve an equation using the division and multiplication properties of equality
  - Solve an equation that requires simplification using the division and multiplication properties of equality
  - Solve an equation involving fractions or decimals using the division and multiplication properties of equality
- Solving Equations using Addition and Subtraction
  - Translate an English sentence to an algebraic equation and solve using the subtraction and addition properties of equality
  - Solve an equation using the subtraction and addition properties of equality
  - Solve an equation that requires simplification using the subtraction and addition properties of equality
  - Solve an equation involving fractions or decimals using the subtraction and addition properties of equality
- Introduction to Inequalities
  - Graph an inequality on the number line
  - Use variables and algebraic symbols to describe inequalities
- Verifying Solutions
  - Determine whether an ordered pair is a solution of a system of linear inequalities
  - Determine whether an ordered pair is a solution of a system of linear equations
  - Verify a solution of an equation - ML

## **Chapter 4: Ratios, Proportions, and Percents**

### 4.1 Ratios and Proportions

- Problem Solving with Ratios
    - Use ratios in applications
    - Translate phrases to expressions as rates or ratios
    - Find unit rates
    - Find unit price
  - Proportions
    - Use the definition of proportion
    - Solve a problem involving proportions
  - Ratios and Fractions
    - Write a ratio as a fraction
    - Write a rate as a fraction
-

## 4.2 Percents

- Writing Percents
  - Convert percents to decimals
  - Convert decimals and fractions to percents
  - Convert between percents, decimals, and fractions
- Introduction to Percents
  - Use the definition of percent
  - Convert percents to fractions
- Financial Applications of Percents
  - Solve sales tax applications
  - Solve mark-up applications
  - Solve discount applications
  - Solve commission applications
  - Determine the final cost of an item including sales tax and discounts
- Applications of Percents
  - Solve basic applications of percent
  - Solve applications of percent
  - Find percent increase and percent decrease
- Percent Equations
  - Write percent equations as proportions
  - Translate and solve percent proportions
  - Translate and solve basic percent equations

## Chapter 5: Functions

### 5.1 Evaluating Functions

- Evaluating Exponential Functions
  - Evaluate exponential functions with base  $e$
  - Evaluate exponential functions
- Function Notation
  - Evaluate a function using function notation
  - Understand function notation

### 5.2 Slopes of Lines

- Slopes of Lines
  - Use the relationship between rise and run to find the slope of a line from its graph
  - Use a geoboard to model slope

### 5.3 Polynomial Functions

- Introduction to Polynomials
    - Identify the types and degrees of polynomials
    - Evaluate a polynomial for a given value
-

- Operations with Polynomials
  - Divide a polynomial by a monomial
  - Divide monomials
  - Multiply monomials
  - Add and subtract monomials

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### Chapter 1: Algebra Reference

#### 1.1 Properties of Real Numbers and Polynomials

- Properties of Real Numbers
  - Use the following properties of real numbers: inverse and identity
  - Use the following properties of real numbers: commutative, associative, and distributive
- Polynomials
  - Add and subtract polynomials
  - Multiply binomials together
  - Multiply polynomials together
  - Perform operations with polynomials of several variables
- Properties of Real Numbers and Order of Operations
  - Distinguish between natural numbers, whole numbers, and integers
  - Distinguish between rational and irrational numbers
  - Perform calculations using order of operations
  - Use the following properties of real numbers: inverse and identity
  - Use the following properties of real numbers: commutative, associative, and distributive
- Evaluate and Simplify Algebraic Expressions
  - Evaluate algebraic expressions with a single variable
  - Evaluate algebraic expressions with two variables
  - Identify constants and variables
  - Use a formula
  - Simplify algebraic expressions

#### 1.2 Factoring

- Factoring Quadratics
    - Factor the greatest common factor of a polynomial
    - Factor a trinomial
    - Factor a trinomial by grouping
    - Factor a perfect square trinomial
    - Factor a difference of squares
  - Other Factoring Techniques
    - Factor a cubic by grouping
    - Factor the sum and difference of cubes
-



- Factor expressions using fractional or negative exponents
- Factor expressions using greatest common factor and other technique

### 1.3 Rational Expressions

- Operations on Rational Expressions
  - Simplify rational expressions
  - Multiply rational expressions
  - Divide rational expressions
  - Add and subtract rational expressions

### 1.4 Equations

- Linear Equations
  - Identify identity, conditional, and inconsistent equations
  - Solve equations in one variable algebraically, variable just on one side
  - Solve equations in one variable algebraically, variable on both sides
- Quadratic Equations
  - Solve quadratic equations by factoring, leading coefficient 1
  - Solve quadratic equations by factoring, leading coefficient  $> 1$
  - Solve quadratic equations by using the quadratic formula
- Rational Equations
  - Solve a rational equation, monomials in denominator
  - Solve a rational equation, binomials in denominator
  - Solve a rational equation, requires factoring to find least common denominator

### 1.5 Inequalities

- Linear Inequalities
  - Use interval notation
  - Use properties of inequalities
  - Solve simple inequalities in one variable algebraically
- Quadratic and Rational Inequalities
  - Solve quadratic inequalities in one variable, graph the solution set, and express the solution set using interval notation
  - Solve inequalities that involve rational expressions, graph the solution sets, and express the solution set using interval notation

### 1.6 Exponents

- Properties of Exponents
    - Understand exponent notation
    - Use the product rule of exponents
    - Use the quotient rule of exponents
    - Use the power rule of exponents
  - Advanced Properties of Exponents
    - Use the negative and zero exponent rule
    - Find the power of a product
-

- Find the power of a quotient
- Simplify exponential expressions

### 1.7 Radicals

- Simplify Radicals
  - Evaluate square roots
  - Use the product rule to simplify square roots
  - Use the quotient rule to simplify square roots
- Operations with Radicals
  - Add and subtract square roots
  - Rationalize denominators with a monomial denominator
  - Rationalize denominators using the conjugate

## Chapter 2: Linear Functions

### 2.1 Slopes and Equations of Lines

- Cartesian Coordinate System
  - Plot ordered pairs in a Cartesian coordinate system
  - Graph equations by plotting points
- Identify Slopes and Intercepts
  - Find the slope of a line given two points
  - Understand the relationship between the slope and y-intercept of a line and its equation
  - Find x -intercepts and y -intercepts
- Finding Linear Equations
  - Find equation of a line, in slope-intercept form, given slope and one point (point-slope formula)
  - Find equation, in slope-intercept form, of a line passing through two given points
  - Given slope and intercept, find the equation of a line and write it in standard form
  - Find the equation of vertical and horizontal lines
- Graphing Linear Equations
  - Graph a linear equation using the slope and the origin
- Parallel and Perpendicular Lines
  - Given the equations of two lines, determine whether their graphs are parallel or perpendicular
  - Write the equation of a line parallel to a given line
  - Write the equation of a line perpendicular to a given line

### 2.2 Linear Functions and Applications

- Linear Functions
    - Understand function notation
    - Evaluate a linear function at a value
-

- Applications of Linear Functions
  - Solve supply and demand problems using linear functions
  - Solve cost analysis problems using linear functions
  - Solve break even analysis problems using linear functions
- Mass and Temperature
  - Identify unit of mass correctly for a given situation
  - Convert between celsius and fahrenheit

### 2.3 The Least Squares Line

- The Least Squares Line
  - Find the linear regression equation given a list of data points
  - Make predictions using a line of best fit
  - Find and interpret the correlation coefficient

## Chapter 3: Systems of Linear Equations and Matrices

### 3.1 Solving Linear Systems

- Linear Systems in Two Variables
  - Solve systems of equations in two variables by graphing
  - Solve systems of equations in two variables by substitution
  - Solve systems of equations in two variables by addition
  - Identify inconsistent and dependent systems of equations containing two variables, and express the solution of dependent equations
- Linear System in Three Variables
  - Determine whether an ordered triple is a solution to a system
  - Solve systems of three equations in three variables
  - Identify inconsistent and dependent systems of equations containing three variables, and express the solution of a system of dependent equations
- Applications of Linear Systems
  - Use systems of equations to investigate profits
  - Write and solve a system of equations in two variables from a word problem

### 3.2 Solving Linear Systems by the Gauss-Jordan Method

- Solving Systems with Gaussian Elimination
  - Convert between a system of equations and its corresponding augmented matrix
  - Use row operations to solve a system of linear equations in two variables
  - Use row operations to solve a system of linear equations in three variables
  - Use matrices to solve applications of systems of linear equations

### 3.3 Operations with Matrices

- Addition and Subtraction of Matrices
    - Determine the order of a matrix and describe elements within a matrix
    - Add or subtract matrices
-

- Multiplication of Matrices
  - Multiply a matrix by a scalar
  - Find the sum or difference of scalar multiples
  - Multiply two matrices

### 3.4 Matrix Inverses and Determinants

- Determinants of Matrices
  - Find the determinant of a 2x2 matrix
  - Find the determinant of a 3x3 matrix
- Inverse and Identity Matrices
  - Understand the identity matrix and how it relates to the inverse matrix
  - Determine if a matrix is invertible using the determinant
  - Find the inverse of a 2x2 matrix
  - Find the inverse of a 3x3 matrix
- Solving Systems with Inverses
  - Solve a system of linear equations using the inverse of a 2x2 matrix
  - Solve a system of linear equations using the inverse of a 3x3 matrix

### 3.5 Input-Output Models

- Input-Output Matrices
  - Create an input output matrix for a given application
  - Calculate the amount of commodities produced given an input output matrix and a production matrix
  - Determine the production matrix that will satisfy a given demand matrix
  - Find the production of a commodity in a closed input output model

## **Chapter 4: Linear Programming - The Graphical Method**

### 4.1 Graphing Linear Inequalities

- Graphs of Linear Inequalities
  - Solve a linear inequality in two variables by graphing
  - Solve a linear system of inequalities by graphing

### 4.2 Solving Linear Programming Problems Graphically

- Solving Linear Programming Problems Graphically
  - Graph a feasible region given a set of constraints
  - Find the maximum value of an objective function given constraints by graphing

### 4.3 Applications of Linear Programming

- Applications of Linear Programming
    - Solve application problems using linear programming
-

## **Chapter 5: Linear Programming - The Simplex Method**

### 5.1 Slack Variables and the Pivot

- Finding Solutions using Initial Simplex Tableaus
  - Rewrite a linear programming problem using slack variables and create an initial simplex tableau
  - Read a solution from an initial simplex tableau
  - Find a new solution by pivoting an initial simplex tableau

### 5.2 Maximization and Minimization Problems

- Solving Maximization Problems with the Simplex Method
  - Solve maximization problems using the simplex method
- Transposing a Matrix and Finding the Dual of a Linear Programming Problem
  - Determine the transpose of a matrix
  - Determine the dual of a linear programming problem
- Solving Minimization Problems with Duality
  - Solve minimization problems using the theorem of duality

### 5.3 Nonstandard Problems

- Solving Nonstandard Problems
  - Solve a nonstandard linear programming problem
  - Solve a nonstandard linear programming application problem

## **Chapter 6: Mathematics of Finance**

### 6.1 Simple Interest

- Simple Interest
  - Calculate simple interest
  - Calculate interest discounts on a discounted loan

### 6.2 Compound Interest

- Compound Interest
    - Calculate periodically compounded interest
    - Calculate compound interest
    - Calculate continuously compounded interest
    - Calculate effective annual yield
  - Geometric Sequences
    - Find the common ratio of a geometric sequence
    - Write terms of a geometric sequence
    - Write a recursive formula for a geometric sequence
    - Write an explicit formula for a geometric sequences
    - Find the sum of a finite geometric sequence
-

### 6.3 Annuities, Stocks, and Bonds

- Annuities
  - Calculate the value of an annuity
  - Calculate the payment needed to achieve a determined future value
- Stocks
  - Define stock terminology
  - Read a stock table

### 6.4 Installment Loans, Amortization, and Credit Cards

- Mortgages and Loans
  - Calculate the monthly payment and interest cost for a mortgage
  - Construct a loan amortization schedule
  - Choose the best installment loan plan
- Credit Cards
  - Recognize key features of credit cards
  - Calculate the average daily balance of a credit card
  - Determine interest to be paid on a card's next billing date

## Chapter 7: Logic

### 7.1 Statements and Logical Connectives

- The Building Blocks of Logic
  - Identify and negate simple statements
  - Identify and negate quantified statements
- Symbolic Representation of Statements
  - Identify logical connectives and compound statements
  - Represent and/or/not statements in symbolic form and English
- Conditional Statements
  - Represent conditional statements in symbolic form and English
  - Write biconditional statements in symbolic form and English
  - Represent symbolic statements with parentheses using dominance of connectives

### 7.2 Truth Tables for Negation, Conjunction, and Disjunction

- Introduction to Truth Tables
    - Construct a truth table for a statement with a conjunction and/or a negation and determine its truth value
    - Construct a truth table for a statement with a disjunction and/or a negation and determine its truth value
    - Construct a truth table for a compound statement with a conjunction and disjunction and determine its truth value
-

### 7.3 Truth Tables for the Conditional and Biconditional

- Truth Tables for Conditional and Biconditional Statements
  - Construct a truth table for a conditional statement and determine its truth value
  - Construct a truth table for a biconditional statement and determine its truth value
- Self-Contradictions, Tautologies, and Implications
  - Identify self-contradictions, tautologies, and implications

### 7.4 Equivalent Statements

- Equivalent Statements and De Morgan's Equivalence Laws
  - Determine if two symbolic statements are equivalent using a truth table
  - Determine if two statements given in English are equivalent using a truth table
  - Determine if two statements are equivalent using De Morgan's laws
- Conditional States and Equivalence
  - Convert a disjunction into an equivalent conditional statement
  - Determine if two conditional statements are equivalent

### 7.5 Symbolic Arguments

- Drawing and Verifying Conclusions
  - Draw a conclusion from a conditional statement
  - Determine if an argument is valid using a truth table
  - Identify and validate the standard forms of arguments

### 7.6 Euler Diagrams and Syllogistic Arguments

- Euler Diagrams and Syllogistic Arguments
  - Identify syllogistic arguments
  - Represent a syllogistic argument with a Euler diagram
  - Determine if a syllogistic argument is valid with a Euler diagram

### 7.7 Switching Circuits

- Switching Circuits and Symbolic Logic
  - Convert between symbolic statements and switching circuits
  - Determine conditions for when a lightbulb will be turned on in a switching circuit
  - Determine if two switching circuits are equivalent

## Chapter 8: Sets and Counting Principles

### 8.1 Set Concepts

- Introduction to Sets and Set Builder Notation
    - Represent a set using a written description and the roster method
    - Represent a set using set builder notation
  - Set Equivalence
    - Identify the cardinal number for a set
    - Determine if two sets are equivalent
    - Determine if two sets are equal
-

- Types of Sets
  - Identify subsets, universal sets, and empty sets
  - Distinguish between finite and infinite sets
- Subsets and Proper Subsets
  - Identify subsets and proper subsets using set notation
  - Determine the number of subsets and proper subsets in a given set

## 8.2 Venn Diagrams and Set Operations

- Representing Sets with Venn Diagrams
  - Illustrate the universal set, a set, and complement of a set using a Venn diagram
  - Illustrate two sets using Venn diagram and set notation
- Set Relationships
  - Determine the complement of a set using Venn diagrams and proper set notation
  - Determine the intersection of two sets using Venn diagrams and set notation
  - Determine the union of two sets using Venn diagrams and set notation
- Set Operations
  - Perform operations on sets
  - Find the difference and cartesian product of two sets
  - Use Venn diagrams to find the result of set operations on two sets
  - Determine the cardinal number of a union of two finite sets

## 8.3 Venn Diagrams with Three Sets and Verification of Equality of Sets

- Construct a Venn Diagram of Three Sets
  - Perform set operations on three sets
  - Represent three sets using Venn diagrams

## 8.4 The Fundamental Counting Principle

- The Fundamental Counting Principle
  - Solve counting problems using the addition principle
  - Solve counting problems using the multiplication principle

## 8.5 Permutations and Combinations

- Permutations
    - Evaluate an expression with factorials
    - Find the number of permutations of  $n$  distinct objects using the multiplication principle
    - Find the number of permutations of  $n$  distinct objects using a formula
    - Find the number of permutations of  $n$  non-distinct objects
  - Combinations
    - Find the number of combinations using the formula
    - Find the number of subsets of a set
-



## Chapter 9: Probability

### 9.1 Introduction to Probability

- Sample Spaces and Events
  - Determine the sample space of an experiment
  - Determine an event of an experiment
- Fundamentals of Probability
  - Compute the probability of equally likely outcomes
  - Compute the probability of equally likely outcomes in application
- Probability with Permutations and Combinations
  - Compute probability involving permutations
  - Compute probability involving combinations
- The Complement Rule and Probability
  - Use the complement rule to compute probabilities
  - Compute the probability of an event happening at least once
- Odds and Expected Value
  - Compute the expected value of an event
  - Compute odds using probability

### 9.2 Conditional Probability and Independent Events

- Independent Events
  - Compute the probability of the union of two events
  - Compute the probability of two independent events occurring
- Dependent Events and Conditional Probability
  - Compute the conditional probability of a dependent event occurring
  - Compute the probability of two or more dependent events occurring

### 9.3 Binomial Probability

- Binomial Experiments
  - Identify a binomial experiment
  - Determine the binomial probability of success in an experiment performed multiple times
  - Calculate expected value for binomial probability

### 9.4 Bayes' Theorem

- Bayes' Theorem
  - Apply Bayes' theorem to solve an application problem

### 9.5 Random Variables, Probability Distributions and Expected Value

- Random Variables, Probability Distributions, and Expected Value
    - Calculate probability distribution
    - Calculate the expected value of a random variable
-

## Chapter 10: Statistics

### 10.1 Sampling, Frequency Distributions, and Graphs

- Sampling and Parameters
  - Understand the definitions of population, sampling, statistic, parameter, and data
  - Identify stratified, cluster, systematic, and convenience sampling
  - Identify sampling errors and bias
  - Identify situations in which statistics can be misleading
- Frequency Distributions and Histograms
  - Construct and understand frequency tables for a set of data
  - Create and interpret histograms
  - Create and interpret stem-and-leaf plots
- Estimation from Graphs/Figures
  - Estimate using a pie chart or bar graph
  - Estimate using a line graph

### 10.2 Measures of Central Tendency and Measures of Dispersion

- Means and Medians
  - Find the mean of a set of data
  - Find the mean from a frequency table
  - Find the median of a set of data
- Modes, Midranges, and Choosing a Measurement
  - Find the mode of a set of data
  - Find the midrange of a set of data
  - Determine whether the mean, median, or mode is the best measure of center for a data set
- Standard Deviation
  - Compute the sample variance and sample standard deviation
  - Interpret the standard deviation of a set of data

### 10.3 The Normal Distribution, Margins of Error, and Skewness

- The Normal Distribution
    - Understand the notation and interpret the parameters of a normal distribution
    - Compute z-scores and use them to compare values from different data sets
    - Determine if a data set is skewed
  - Percentiles, Quartiles, and Margins of Error
    - Find and interpret percentiles and quartiles of a data set
    - Calculate and interpret margin of error
  - Problem Solving with the Normal Distribution
    - Standardize a normally distributed random variable
    - Calculate the mean and standard deviation of a standard normal distribution
-

## Chapter 11: Nonlinear Functions

### 11.1 Properties of Functions

- Functions and Function Notation
  - Identify domain and range from a set of ordered pairs
  - Determine whether a relation represents a function
- Relations and Functions
  - Determine whether a function is one-to-one
  - Use the vertical line test to identify functions
  - Use the horizontal line test to identify one-to-one functions

### 11.2 Quadratic Functions

- Characteristics of Parabolas
  - Determine axis of symmetry and vertex of parabolas from a graph
  - Determine x- and y-intercepts of parabolas from a graph
- Graphs of Quadratic Functions
  - Find the direction a parabola opens and its axis of symmetry and vertex from the general form of its equation
  - Identify the axis of symmetry and vertex of a parabola from its equation in standard form
  - Write the equation of a quadratic function given vertex and a point on a graph
  - Write the equation of a quadratic function given intercepts on a graph
  - Write the equation of a quadratic function in standard form given the equation in general form
- Applications of Quadratic Functions
  - Find the domain and range of a quadratic function
  - Determine the maximum and minimum values of quadratic functions
  - Find the x- and y-intercepts of a quadratic function

### 11.3 Transformations of Functions

- Transformations of Functions
  - Graph functions using vertical and horizontal shifts
  - Graph functions using reflections about the x-axis and the y-axis
  - Graph functions using compressions and stretches
  - Combine transformations

### 11.4 Polynomial and Rational Functions

- Polynomial Functions
    - Identify power functions and polynomial functions
    - Graph polynomial functions
    - Write a formula for a polynomial function from a graph
    - Determine equation of a polynomial given key information
-

- Asymptotic Behavior of Rational Functions
  - Use arrow notation to describe local behavior and end behavior of rational functions
  - Identify vertical asymptotes and removable discontinuities of rational functions
  - Identify horizontal and slant asymptotes of rational functions
- Graphs and Applications of Rational Functions
  - Find the intercepts of a rational function
  - Graph rational functions
  - Find the equation of a rational function from a graph

#### 11.5 Exponential and Logarithmic Functions

- Identify and Evaluate Exponential Functions
    - Identify exponential functions
    - Evaluate exponential functions
    - Calculate continuous growth and decay
  - Graphing Exponential Functions
    - Graph exponential functions
    - Graph exponential functions using transformations
  - Relate Logarithms and Exponents
    - Convert from logarithmic to exponential form
    - Convert from exponential to logarithmic form
  - Evaluate Logarithmic Expressions
    - Evaluate logarithms with positive integer solutions
    - Evaluate logarithms with negative integer solutions
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    - Use natural logarithms
  - Basic Properties of Logarithms
    - Understand the basic properties of logarithms
    - Use the product rule for logarithms
    - Use the quotient rule for logarithms
    - Use the power rule for logarithms
  - Solve Logarithmic Equations
    - Use the definition of a logarithm to solve logarithmic equations
    - Use logarithm properties and the definition of the logarithm to solve logarithmic equations
    - Use the one-to-one property of logarithms to solve logarithmic equations
  - Applications of Exponential and Logarithmic Functions
    - Model exponential growth
    - Model exponential decay
    - Applied logarithmic models
    - Choose an appropriate model for data
    - Express an exponential model in base  $e$
-

## Chapter 12: Markov Chains

### 12.1 Properties of Markov Chains

- Transitions
  - Identify transition diagrams and transition matrices
  - Create a transition diagram and matrix for a given word problem
- States
  - Find the second state of a system given a transition matrix and initial state
  - Find powers of a transition matrix
  - Solve application problems using powers of transition matrices

### 12.2 Regular Markov Chains

- Regular Transition Matrices and Stationary Matrices
  - Determine if a transition matrix is regular
  - Find a stationary matrix for a given transition matrix
  - Solve application problems using stationary matrices

### 12.3 Absorbing Markov Chains

- Absorbing States
    - Find absorbing states given a transition matrix
    - Determine if a transition matrix is for an absorbing Markov chain
    - Write a transition matrix in standard form
  - Limiting Matrix
    - Find the limiting matrix for an absorbing Markov chain
-