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Intermediate Algebra

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Alta Intermediate Algebra was developed to meet the scope and sequence of a typical one-semester algebra course. To develop the course, Knewton used three main sources of content: OpenStax, videos created by a Math Professor we have partnered with, and a team of Subject Matter Experts. The SMEs come from diverse backgrounds and are all academics in the field of mathematics.

Alta Intermediate Algebra has two instructional sequences for every learning objective, giving students multiple opportunities to learn new concepts. Between our OpenStax text, video content, and Knewton SMEs, we were able to solicit ideas from math instructors and students at all levels of higher education. Alta Intermediate Algebra covers the typical breadth of algebra topics, and also provides the necessary depth to ensure the course is manageable and engaging for instructors and students alike.

Intermediate Algebra | Table of Contents

Chapter 1: Foundations
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    - Translate an English phrase and word problems into an algebraic expression

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    - Identify conic sections by their equations

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12.2 Arithmetic Sequences and Series

- Arithmetic Sequences and Series
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- Geometric Sequences
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