

### **Business Calculus | Table of Contents**

## **Chapter 1: Linear Equations and Graphs**

### 1.1 Linear Equations and Inequalities

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- 3.1 Introduction to Limits
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    - Evaluate limits graphically
    - Understand the properties of limits



- Limits Analytically for Continuous and Piecewise Functions
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  - Evaluate limits analytically for piecewise functions
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- Limits Analytically for Functions with Removable Discontinuities
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  - Evaluate two-sided limits analytically for rational functions that contain radicals with removable discontinuities

## 3.2 Infinite Limits and Limits at Infinity

- Infinite Limits
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  - Evaluate limits of radical and exponential functions at infinity

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- Continuity and the Intermediate Value Theorem
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  - Understand and apply the intermediate value theorem
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  - Determine the value that makes a piecewise function continuous
- Rational and Quadratic Inequalities
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### 3.4 The Derivative

- Secant Lines and Average Rates of Change
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  - Find the average rate of change given a function and variable intervals
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- Estimate the instantaneous rate of change of a function from successively closer approximations
- The Definition of the Derivative
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    - Use properties of logarithms to find the derivative of a natural logarithmic function
  - Derivatives of Logarithmic Functions of Any Base
    - Find the derivative of a logarithmic function that is not base e
    - Use properties of logarithms to find the derivative of a logarithmic function that is not base e



- Logarithmic Differentiation
  - Use logarithmic differentiation
  - Use logarithmic differentiation with all properties of logarithms

### 4.2 Derivatives of Products and Quotients

- The Product and Quotient Rules
  - Use the product rule to find the derivative of a function in the form f(x)g(x)
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  - Use the product rule to find the derivative of a function in the form f(x)g(x)h(x)
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- The Product and Quotient Rules with Exponential Functions
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  - Use product and quotient rules to find the derivative of exponential functions with any base

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- Using the Chain Rule
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  - Use the chain rule with the product and quotient rules

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### 4.6 Elasticity of Demand

- Relative Rate of Change and Elasticity of Demand
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  - Interpret elasticity of demand



## **Chapter 5: Graphing and Optimization**

## 5.1 First Derivative and Graphs

- First Derivative Test
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  - Use the first derivative test to find local extrema from a graph
  - Use the first derivative test to find local extrema given a function
- The Graph of the Derivative Function
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  - Determine the open intervals where the first derivative is positive or negative from a graph
  - Determine the graph of the derivative function given the graph of a polynomial function

# 5.2 Second Derivative and Graphs

- Concavity and the Second Derivative Test
  - Determine concavity and find the inflection points from a graph of f(x)
  - Determine concavity and find the inflection points given a function
  - Use the second derivative test to find local extrema given a function

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- Using L'Hospital's Rule
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  - Apply L'Hospital's Rule in the (infinity/infinity) case
  - Determine when to apply L'Hospital's Rule

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  - Sketch the graph of a function with a cusp

### 5.5 Absolute Maxima and Minima

- Extreme Value Theorem and Absolute Extrema
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  - Locate local and absolute extrema from a graph
  - Locate critical points using derivatives
  - Locate absolute extrema

## 5.6 Optimization

- Applied Optimization Problems
  - Maximize or minimize area or volume
  - Minimize travel time
  - Maximize revenue
  - Minimize surface area



- Optimization Problems in the Abstract
  - Maximize the area of an inscribed rectangle
  - Maximize and minimize quantities given an expression with two variables
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- Differential Equations for Growth and Decay
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### 6.4 The Definite Integral

- Left and Right Riemann Sums
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- Midpoint and Trapezoid Rule
  - Approximate the area under a curve using midpoint approximation
  - Approximate the area under a curve using trapezoidal approximation
- Defining Definite Integrals
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  - Evaluate definite integrals with the Fundamental Theorem of Calculus and the power rule by simplifying
- Average Value of a Function
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## **Chapter 7: Additional Integration Topics**

### 7.1 Area Between Curves

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  - Find the area of a region bounded between a linear function and another function
  - Find the area of a region bounded between two curves
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  - Find the area of a region bounded above by two different functions
- Applications of Area Between Curves
  - Find and interpret the Gini index



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  - Find the future value of a continuous stream
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  - Find the consumers' surplus at a certain price level
  - Find the producers' surplus at a certain price level
  - Find the equilibrium price and the consumers' and producers' surplus at that price

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  - Find the partial derivative of a function of three variables



- Higher Order Partial Derivatives
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## 8.6 Double Integrals over More General Regions

- Double Integrals Over Nonrectangular Regions
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- Applications of Double Integrals Over General Regions
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    - Use right triangles to evaluate sin, cos, and tan functions
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- Recognizing and Solving First-order Linear Differential Equations
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## **Chapter 11: Taylor Polynomials and Sequences and Series**

# 11.1 Taylor Polynomials

- Taylor and Maclaurin Polynomials
  - Recognize a Taylor series
  - Find the Taylor polynomials for a function at a value



## 11.2 Taylor Series

- Representing Functions with Taylor and Maclaurin Series
  - Represent a function at a value with a Taylor series and determine the interval of convergence
  - Find the Maclaurin series for a function and show that the series converges

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- Finding the Maclaurin Series that Represents a Function
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  - Estimate a trigonometric function value using Maclaurin polynomials
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- Geometric Sequences
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  - Write terms of a geometric sequence
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  - Find the equivalent fraction for a repeating decimal
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- Finite and Infinite Geometric Series
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- Improper Integrals over Infinite Intervals
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- Probability Density Functions
  - Understand the properties of probability density functions
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- Other Parameters of Probability Density Functions
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  - Compute z-scores and use them to compare values from different data sets
  - Use a table to find probabilities in a normal distribution