

## Foundations of Mathematics | Table of Contents

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### **Chapter 15: Rational Expressions and Equations**

#### 15.1 Simplify Rational Expressions

- Domain of Rational Expressions and Simplifying Rational Expressions
  - Determine the values for which a rational expression is undefined (20)
  - Evaluate a rational expression (20)
  - Simplify a rational expression (20)
  - Simplify a rational expression with opposite factors (20)

#### 15.2 Multiply and Divide Rational Expressions

- Multiplying and Dividing Rational Expressions
  - Multiply rational expressions (20)
  - Divide rational expressions (20)
  - Multiply and divide more than two rational expressions (20)

#### 15.3 Add and Subtract Rational Expressions with a Common Denominator

- Adding and Subtracting Rational Expressions with a Common Denominator
  - Add rational expressions with a common denominator (20)
  - Subtract rational expressions with a common denominator (20)
  - Add and subtract rational expressions whose denominators are opposites (20)

#### 15.4 Add and Subtract Rational Expressions with Unlike Denominators

- Adding and Subtracting Rational Expressions with Unlike Denominators
    - Find the least common denominator of rational expressions (20)
    - Find equivalent rational expressions (20)
    - Add rational expressions with different denominators (20)
    - Subtract rational expressions with different denominators (20)
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### 15.5 Simplify Complex Rational Expressions

- Simplifying Complex Fractions
  - Simplify a complex rational expression by writing it as division (20)
  - Simplify a complex rational expression by using the LCD

### 15.6 Solve Rational Equations

- Solving Rational Equations
  - Solve a rational equation that results in a linear equation
  - Solve a rational equation that results in a quadratic equation
  - Solve a rational equation for a specific variable

### 15.7 Solve Proportion and Similar Figure Applications

- Proportions and Problem Solving with Rational Equations
  - Solve proportions (20)
  - Solve applications with proportions
  - Solve similar figure applications

### 15.8 Solve Uniform Motion and Work Applications

- Uniform Motion, Work, and Problem Solving
  - Solve uniform motion applications involving rational equations
  - Solve problems involving rates of work using rational equations

### 15.9 Use Direct and Inverse Variation

- Variation and Problem Solving
  - Solve direct variation problems
  - Solve inverse variation problems

### 15.10 Solve Rational Inequalities

- Solving Rational Inequalities
  - Find the solution set of a rational inequality
  - Solve an inequality with rational functions (40)

## **Chapter 16: Roots and Radicals**

### 16.1 Simplify and Use Square Roots

- Understanding Square Roots
  - Simplify expressions with square roots (20)
  - Estimate square roots and approximate square roots (20, 20)
  - Simplify variable expressions with square roots (20)

### 16.2 Simplify Square Roots

- Simplifying Square Root Expressions
  - Use the product property to simplify square roots
  - Use the quotient property to simplify a perfect square fraction (20)
  - Use the quotient property to simplify square roots

### 16.3 Add and Subtract Square Roots

- Adding and Subtracting Square Root Expressions
  - Add and subtract like square roots (20)
  - Add and subtract square roots that need simplification (20)

### 16.4 Multiply Square Roots

- Multiplying Square Root Expressions
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- Multiply square roots (20)
- Use polynomial multiplication to multiply square roots (20)
- Use special product formulas to multiply square roots (20)

#### 16.5 Divide Square Roots

- Dividing Square Root Expressions and Rationalizing Denominators
  - Divide square roots (20)
  - Rationalize a one-term denominator (20)
  - Rationalize a two-term denominator (20)

#### 16.6 Solve Equations with Square Roots

- Solving Radical Equations
  - Solve a square root equation with a single radical (20)
  - Solve a square root equation with two radicals (20)
  - Use square roots in applications

#### 16.7 Higher Roots

- Understanding Higher Roots
  - Simplify numerical expressions with higher roots
  - Simplify expressions with higher roots (20)
- Simplifying Higher Roots and Operations on Higher Roots
  - Use the product property to simplify expressions with higher roots
  - Use the quotient property to simplify expressions with higher roots
  - Add and subtract higher roots (20)

#### 16.8 Rational Exponents

- Simplifying Expressions with Rational Exponents
  - Simplify expressions with rational exponents and a numerator of 1 (20)
  - Simplify expressions with rational exponents and a numerator greater than 1 (20)
  - Use the laws of exponents to simplify expressions with rational exponents

#### 16.9 Use Radicals in Functions

- Radical Functions
  - Evaluate a radical function (20)
  - Find the domain of a radical function
  - Graph a radical function by plotting points and determine its range

#### 16.10 Use the Complex Number System

- Introduction to Complex Numbers
  - Evaluate the square root of a negative number and understand the complex number system (20)
  - Add or subtract complex numbers (20)
- Multiplying and Dividing Complex Numbers and Powers of  $i$ 
  - Multiply complex numbers (20)
  - Multiply two complex conjugates (20)
  - Divide complex numbers (20)
  - Simplify powers of  $i$  (20)

### **Chapter 17: Quadratic Equations**

#### 17.1 Solve Quadratic Equations Using the Square Root Property

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- Solving Quadratic Equations Using the Square Root Property
  - Solve a quadratic equation using the square root property (20)
  - Solve a quadratic equation with a binomial as the quadratic term using the square root property
  - Solve a quadratic equation where factoring results in a perfect square binomial

#### 17.2 Solve Quadratic Equations by Completing the Square

- Solving Quadratic Equations by Completing the Square
  - Complete the square of a binomial expression (20)
  - Solve a quadratic equation with a leading coefficient of 1 by completing the square (20)
  - Solve a quadratic equation with a leading coefficient greater than 1 by completing the square (20)

#### 17.3 Solve Quadratic Equations Using the Quadratic Formula

- Solving Quadratic Equations with the Quadratic Formula
  - Solve a quadratic equation using the quadratic formula with 2 real solutions (20)
  - Solve a quadratic equation using the quadratic formula with 1 or 0 real solutions (20)
  - Use the discriminant to predict the number of solutions of a quadratic equation (20)

#### 17.4 Solve Quadratic Equations in Quadratic Form

- Solving Equations by Using Quadratic Methods
  - Solve an equation in quadratic form by using substitution (40)
  - Solve an equation in quadratic form with rational or negative exponents by using substitution (40)

#### 17.5 Solve Applications Modeled by Quadratic Equations

- Problem Solving with Quadratic Equations
  - Solve applications modeled by quadratic equations that may require the quadratic formula
  - Solve geometric applications that may require the quadratic formula

#### 17.6 Graph Quadratic Functions Using Properties

- Parabolas and Their Properties
  - Graph a quadratic function by plotting points and determine the direction a parabola opens
  - Determine the axis of symmetry and vertex of a parabola given a function (20)
  - Determine the intercepts of a parabola given a function (20)
- Graphing Quadratic Functions
  - Graph a quadratic function by finding key points
  - Determine the minimum or maximum of a quadratic function and use it in applications (40)

#### 17.7 Graph Quadratic Functions Using Transformations

- Transformations of Parabolas
  - Graph a quadratic function using a vertical translation
  - Graph a quadratic function using a horizontal translation
  - Graph a quadratic function by compression, stretching, or reflecting
- Graphing Quadratic Functions Using Transformations
  - Rewrite a quadratic in vertex form and graph it using transformations
  - Find a quadratic function given its graph

#### 17.8 Solve Quadratic Inequalities

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- Solving Quadratic Inequalities
  - Solve a quadratic inequality graphically
  - Solve a quadratic inequality algebraically (40)

## **Chapter 18: Exponential and Logarithmic Functions**

### **18.1 Finding Composite and Inverse Functions**

- Composite Functions
  - Perform a composition of functions (20)
  - Evaluate a composition of functions for a specific value (20)
- One-to-One Functions
  - Determine whether a function is one-to-one given a set of ordered pairs
  - Use the horizontal line test to determine whether a graph represents a one-to-one function
- Inverse Functions
  - Find the inverse of a function given a set of ordered pairs or a graph (40)
  - Verify that two functions are inverses of each other (40)
  - Find the inverse of a function algebraically (40)

### **18.2 Evaluate and Graph Exponential Functions**

- Graphing Exponential Functions
  - Graph an exponential function and understand its properties
  - Graph an exponential function using transformations
  - Evaluate an exponential function with base  $e$  and understand the natural base (40)
- Applications with Exponential Functions
  - Use the one-to-one property of exponential equations to solve an exponential equation (40)
  - Use the compound interest formula to find the new value of an account (40)
  - Use the continuously compounding interest formula to find the new value of an account (40)
  - Calculate resultant values using exponential growth and decay models (40)

### **18.3 Evaluate and Graph Logarithmic Functions**

- Introduction to Logarithms
  - Convert between exponential and logarithmic form (20, 20)
  - Evaluate a logarithmic function (20)
- Logarithmic Functions and Applications
  - Graph a logarithmic function and understand its properties
  - Solve a logarithmic equation by rewriting the equation in exponential form (20)
  - Use logarithmic models in applications (40)

### **18.4 Use the Properties of Logarithms**

- Understanding the Properties of Logarithms
    - Use basic properties of logarithms and the inverse properties of logarithms (40)
    - Use the product, quotient, and power properties of logarithms (40)
  - Using the Properties of Logarithms
    - Use the properties of logarithms to expand a logarithmic expression (40)
    - Use the properties of logarithms to condense a logarithmic expression (40)
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- Use the change-of-base formula for logarithms (20)

#### 18.5 Solve Exponential and Logarithmic Equations

- Solving Logarithmic Equations
  - Use the one-to-one property of logarithmic equations to solve logarithmic equations (40)
  - Use the properties of logarithms to solve logarithmic equations (40)
- Solving Exponential Equations and Applications
  - Solve exponential equations using logarithms (40)
  - Solve for amounts other than a new balance with the compound or continuously compounding interest formula (40)
  - Use the exponential growth and decay models to find values other than the resultant value (40)

### Chapter 19: Conics

#### 19.1 Distance and Midpoint Formulas and Circles

- The Distance and Midpoint Formulas
  - Use the distance formula to find the distance between two points (20)
  - Use the midpoint formula to find the midpoint between two points
- The Equation of Circles
  - Write the standard form of the equation of a circle given its center and radius (20)
  - Write the standard form of the equation of a circle given its center and a point on the circle (20)
  - Graph a circle given its equation in standard form
  - Rewrite the equation of a circle given in general form by completing the square

#### 19.2 Parabolas

- Parabolas as Conic Sections and Applications
  - Graph a vertical parabola given the equation in general or standard form
  - Graph a horizontal parabola given the equation in general form
  - Graph a horizontal parabola given the equation in standard form
  - Solve applications with parabolas

#### 19.3 Ellipses

- Ellipses with Centers at the Origin
  - Graph an ellipse with its center at the origin
  - Find the equation of an ellipse with its center at the origin
- Ellipses with Centers Not at the Origin and Applications
  - Graph an ellipse with its center not at the origin
  - Rewrite the equation of an ellipse given in general form by completing the square
  - Solve applications with ellipses

#### 19.4 Hyperbolas

- Hyperbolas as Conic Sections
    - Graph a hyperbola with its center at the origin
    - Graph a hyperbola with its center not at the origin
    - Rewrite the equation of a hyperbola given in general form by completing the square
  - Identifying Conic Sections by Their Equations
    - Identify conic sections by their equations
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### 19.5 Solve Systems of Nonlinear Equations

- Solving Systems of Nonlinear Equations
  - Solve a system of nonlinear equations by graphing
  - Solve a system of nonlinear equations using substitution (40)
  - Solve a system of nonlinear equations using elimination (40)
- Problem Solving with Systems of Nonlinear Equations
  - Use a system of nonlinear equations to solve applications (40)

## Chapter 20: Sequences, Series, and the Binomial Theorem

### 20.1 Sequences

- Introduction to Sequences
  - Write the first few terms of a sequence (20)
  - Find a formula for the general term of a sequence (20)
- Factorial Notation and Sigma Notation
  - Use factorial notation (20)
  - Find the partial sum (20)
  - Use summation notation to write a sum (20)

### 20.2 Arithmetic Sequences and Series

- Arithmetic Sequences and Series
  - Determine if a sequence is arithmetic and write the first few terms of an arithmetic sequence (20)
  - Find the general term of an arithmetic sequence (20)
  - Find the sum of the first  $n$  terms of an arithmetic sequence (20)

### 20.3 Geometric Sequences and Series

- Geometric Sequences
  - Determine if a sequence is geometric and write the first few terms of a geometric sequence (20)
  - Find the general term of a geometric sequence (20)
- Finite and Infinite Geometric Series and Applications
  - Find the sum of the first  $n$  terms of a geometric sequence (20)
  - Find the sum of an infinite geometric series and use infinite geometric series to write a repeating decimal as a fraction (20, 20)
  - Use geometric sequences and series to solve monetary applications including annuities (40)

### 20.4 Binomial Theorem

- The Binomial Theorem
    - Use Pascal's Triangle to expand a binomial (20)
    - Evaluate a binomial coefficient (20)
    - Use the binomial theorem to expand a binomial (20)
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